Suppose we are interested in how the exercise and body mass index affect on the blood pressure. A random sample of 10 males 50 years of age is selected and their height, weight, number of hours of exercise and the blood pressure are measured. Body mass index is calculated by the following fomula.

BMI = ^{(w}	eight in pounds * 703)		
(kg/m²)	height in inches ²		

The dataset is available at U:_MT Student File Area\hjkim\STAT380\SPSS tutorial\blood pressure.sav.

				🚰 Linear Regression
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8:	j			Pre <u>v</u> ious Next
	exercise	bloodpressure	bodymassind ex	Independent(s):
1	4	120	18.4	V bodymassindex
2	10	110	20.1	
3	2	120	22.4	Method: Enter
4	3	135	25.9	Selection Variable:
5	3	140	26.5	Rule
6	5	115	28.9	Case Labels:
7	1	150	30.4	
8	2	165	32.9	WLS Weight:
9	2	160	33.0	
10	0	180	34.7	OK <u>P</u> aste <u>R</u> eset Cancel Help

Select Analyze-Regression-Linear from the pull-down menu.

Placing the variable we would like to predict, blood pressure, in the dependent variable and the variable we will use for prediction, exercise and body mass index in the independent variable, we hit OK. This generates the following SPSS output.

Model Summary ^b					
Model	R	R Square	Adjusted R Square	Std. Error of the Estimate	
1	.897 ^a	.804	.748	11.910	

a. Predictors: (Constant), bodymassindex, exercise

b. Dependent Variable: bloodpressure

	ANOVA [®]						
Model		Sum of Squares	df	Mean Square	F	Sig.	
1	Regression	4079.550	2	2039.775	14.380	.003 ^a	
	Residual	992.950	7	141.850			
	Total	5072.500	9				

a. Predictors: (Constant), bodymassindex, exercise

b. Dependent Variable: bloodpressure

		Unstandardized Coefficients		Standardized Coefficients		
Mode	1	В	Std. Error	Beta	t	Sig.
1	(Constant)	74.491	29.411		2.533	.039
	exercise	-2.835	1.862	332	-1.523	.172
	bodymassindex	2.712	.914	.647	2.965	.021

Coefficients^a

a. Dependent Variable: bloodpressure

The interpretation of R² is same as before. We can see that 80.4% of the variation in Y is explained by the regression line. The fitted regression model found from the output is $\hat{Y} = 74.491 - 2.835X_{\perp} + 2.712X_{2}$

The next part of the output is the statistical analysis (ANOVA-analysis of variance) for the regression model. The ANOVA represents a hypothesis test with where the null hypothesis is $H_{a}: \beta_{i} = 0$ for all i (In simple regression, i = 1)

 $H_A: \beta_i \neq 0$ for at least 1 coefficient

In this example, p-value for this overall test is .003 concluding at least one of independent variables is significantly meaningful to explain the blood pressure.

The individual t-test can also be performed.

$$H_o: \beta_1 = 0 \qquad H_A: \beta_1 \neq 0$$
$$H_o: \beta_2 = 0 \qquad H_A: \beta_2 \neq 0$$

In this example p-value is .172 and .021. Thus, β_1 is not significantly different from zero when body mass index is in the model, and β_2 is significantly different from zero when body mass index is in the model.

Model assumption checking and prediction interval can be done in the similar manner as the simple regression analysis. Normal probability plot and residual plot can be obtained as follows.



Model selection (Variable selection)

🖬 Linear Regression		
 ✓ exercise ✓ bodymassindex ✓ Unstandardized Predict ✓ Standardized Residual [Dependent:	Statistics Plots Save Options
	Method:	
	Selection Variable: Stepwise Remove	
	Sease Labels: Backward Forward	
	WLS Weight:	
ок	Paste Reset Cancel Help	

For variable selection procedure we can choose stepwise, remove, backward, and forward. This procedure automatically selects variables that are significantly important in the model using different procedure. The detail procedure can be found in class handout.

Even though it is not provided in SPSS, model selection criteria such as AIC AICc, BIC, and Cp are also very commonly used to choose the best candidate model.